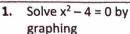
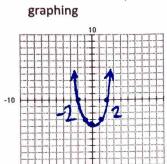
Algebra 2 2B Day 02: Complex Numbers

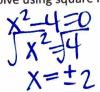




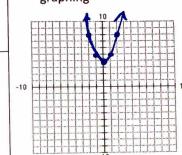
Solve by factoring:

(X+2)(X-2)=0 x = -2 x = 2

Solve using square roots:



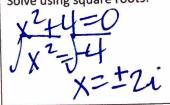
Solve $x^2 + 4 = 0$ by graphing



Solve by factoring:

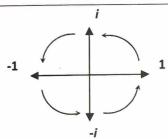
Juesn't factor!

Solve using square roots:



Equations like #2 above is what led mathematicians to DEFINE imaginary numbers. Imaginary numbers were first mentioned back in the 1st Century AD, but Leonhard Euler is the mathematician who introduced the symbol *i* to represent $\sqrt{-1}$ in the 1700's. Imaginary numbers "are non-real, but they are still numbers!" Since these numbers have been defined, we can now solve problems when they are involved.

Imaginary numbers can be thought of a ROTATION of a real number on the number line. Just like the negative numbers represent direction (right is positive, left is negative), i is a 90° rotation. Multiplying by i twice (i²) gets you to -1 multiplying by i four times (i4) gets you back to +1.

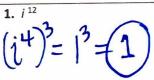


This is the "Argand plane" and it represents the powers of i.

EVALUATING In:

EVALUATING 7:			
j 1	$\sqrt{-1} = i$	i ⁵	i
j ²	$\sqrt{-1} \bullet \sqrt{-1} = -1$	i ⁶	-1
i ³	$\sqrt{-1} \bullet \sqrt{-1} \bullet \sqrt{-1} = -1 \bullet \sqrt{-1} = -i$	i ⁷	-i
i 4	$\sqrt{-1} \bullet \sqrt{-1} \bullet \sqrt{-1} \bullet \sqrt{-1} = (-1)(-1) = 1$	i ⁸	1

See the pattern and find:



Imaginary Number (i): because of the property above, the imaginary number also allows us to take the square root of negative numbers. i is definded as the principal square root of -1:

- $i = \sqrt{-1}$
- $i^2 = -1$

- i is NOT a variable.
- Use i as you would any constant.
- i is NOT a real number...it is called imaginary not because it does not exist, but because many mathematicians refused to believe in it at first.
 - "Imaginary" was meant as a derogative term!!

Pure Imaginary Numbers: square roots of negative real #s.

 $\sqrt{-b^2} = \sqrt{b^2} \cdot \sqrt{-1} = bi$

Complex Number: a number that can be written in the form a + bi, where a and b are real #s and i is the imaginary unit.

Examples: 5 + i and 1 - 7i

Complex Conjugate Pair: 2 solutions are complex numbers. One is a + bi and the other is a - bi

Examples: $\frac{-4 \pm 6i}{3} = -2 + 3i$ and -2 - 3i

SIMPLIFYING RADICALS: A radical is in simplest form when all exponents are positive, no perfect square factor or fraction is left under the radical, and no radicals are in the denominator.

$\sqrt{120}$ **Perfect Square Factorization** $\sqrt{75}$ Since 24 has a factor that's perfect, then break it down as a product of factors and simplify rational factors. $\sqrt{24} = \sqrt{4} \cdot \sqrt{6} = 2\sqrt{6}$ Perfect Squares: 4, 9, 16, 25, 36, 49, . . . SIMPLIFYING IMAGINARY NUMBERS: **2.** $\sqrt{-9}$ **1.** $\sqrt{-5}$ i 19 ist = ist. 52 6152 6. $\sqrt{-80}$ 4. $\sqrt{-32}$ $5.\sqrt{-3}\cdot\sqrt{-12}$ i 516.52 i 53. i 14.3 ADDING AND SUBTRACTING IMAGINARY NUMBERS: 8. (-12 – 3i) – (-3 – 6i) 9. 2i(3+i)+(2-3i)7. (3+5i)+(-2+i)-12-31 6i+2i2+2-31 6i+2(-1)+2-3i 6i-3i-2+2 MULTIPLYING IMAGINARY NUMBERS: There will never be an imaginary answer with a power above 10. 3i · 8i 11. -i(-2 + 10i)2i-10i2 21-106-1) **14.** -2*i* (3 – 2*i*) -6i +41 -6i +4(7) 4-(-1)-21+21 16. (2i)3 (5i) 17. (-4i)(2i)(-9i) 21.21.21.51 Tai +28i -28V -812(-9i) 8.5.12.12 40 (-1)(-1)