

### 1-3 Solving Linear Equations Review

**Properties of Equality** To solve equations, we can use properties of equality.

<b>Addition and Subtraction Properties of Equality</b>	For any real numbers $a$ , $b$ , and $c$ , if $a = b$ , then $a + c = b + c$ and $a - c = b - c$ .
<b>Multiplication and Division Properties of Equality</b>	For any real numbers $a$ , $b$ , and $c$ , if $a = b$ , then $a \cdot c = b \cdot c$ and, if $c \neq 0$ , $\frac{a}{c} = \frac{b}{c}$ .

**Example 1: Solve  $10 - 8x = 50$ .**

$$\begin{aligned}
 10 - 8x &= 50 && \text{Original equation} \\
 10 - 8x - 10 &= 50 - 10 && \text{Subtract 10 from both sides.} \\
 -8x &= 40 && \text{Simplify.} \\
 x &= -5 && \text{Divide both sides by -}
 \end{aligned}$$

**Example 2: Solve  $4x + 5y = 100$  for  $y$ .**

$$\begin{aligned}
 4x + 5y &= 100 && \text{Original equation} \\
 4x + 5y - 4x &= 100 - 4x && \text{Subtract 4x from both sides.} \\
 5y &= 100 - 4x && \text{Simplify.} \\
 y &= \frac{1}{5}(100 - 4x) && \text{Divide both sides by 5.}
 \end{aligned}$$

**Solve each equation (on separate paper if you need more space). Check your solution.**

1.  $\frac{3s}{3} = \frac{45}{3}$   $s = 15$

2.  $17 = 9 - a$   
 $\frac{-9}{-1} = \frac{-9}{-1}$   
 $8 = -a$   
 $a = -8$

3.  $5t - 1 = 6t - 5$   
 $\frac{-5t}{+5} = \frac{-5t}{+5}$   
 $-1 = t - 5$   
 $+5 = +5$   
 $t = 4$

$\frac{3}{2} \cdot \frac{2}{3} m = \frac{1}{2} \cdot \frac{3}{2}$   
 $m = \frac{3}{4}$

5.  $-8 = -2(z + 7)$   
 $-8 = -2z - 14$   
 $6 = -2z$   
 $z = -3$

6.  $3x + 17 = 5x - 13$   
 $17 = 2x - 13$   
 $30 = 2x$   
 $x = 15$

7.  $120 - \frac{3}{4}y = 60$   
 $-\frac{4}{3}(-\frac{3}{4}y + (-60)) = -\frac{4}{3}(-60)$   
 $y = 80$

8.  $\frac{5}{2}n = 98 - n$   
 $\frac{5}{2}n + \frac{2}{2}n = 98$   
 $\frac{7}{2}n = 98$   
 $n = 28$

9.  $4.5 + 2p = 8.7$   
 $2p = 4.2$   
 $p = 2.1$

**Solve each equation or formula for the specified variable (on separate paper if you need more space).**

10.  $a = 3b - c$ , for  $b$   
 $\frac{a+c}{3} = \frac{3b}{3}$   
 $b = \frac{a+c}{3}$  or  $\frac{1}{3}a + \frac{1}{3}c$

11.  $\frac{s}{2t} = 10$ , for  $t$   
 $s = 20t$   
 $t = \frac{s}{20}$

12.  $2xy = x + 7$ , for  $x$   
 $2xy - x = 7$   
 $x(2y - 1) = 7$   
 $x = \frac{7}{2y-1}$

13.  $\frac{d}{2} + \frac{f}{4} = 6$ , for  $f$   
 $4(\frac{f}{4}) = (6 - \frac{d}{2})4$   
 $f = 24 - 2d$

14.  $3(2j - k) = 108$ , for  $j$   
 $2j - k = 36$   
 $2j = k + 36$   
 $j = \frac{k+36}{2}$  or  $\frac{1}{2}k + 18$

15.  $\frac{m}{n} + 5m = 20$ , for  $m$   
 $m(\frac{1}{n} + 5) = 20$   
 $m = \frac{20}{\frac{1}{n} + 5}$   
 See L.L. for more...

$$15. \frac{m}{n} + 5m = 20$$

$$\frac{m}{n} + \frac{5mn}{n} = 20$$

$$\frac{m + 5mn}{n} = 20$$

$$m + 5mn = 20n$$

$$m(1 + 5n) = 20n$$

$$m = \frac{20n}{1 + 5n}$$

😊 Much better!

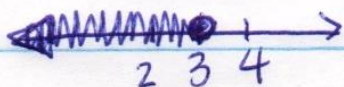
### 1-5 Solving Linear Inequalities Review

$$1. 7(7a - 9) \leq 84$$

$$49a - 63 \leq 84$$

$$49a \leq 147$$

$$a \leq 3$$

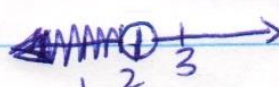


$$2. 3(9z + 4) > 35z - 4$$

$$27z + 12 > 35z - 4$$

$$16 > 8z$$

$$2 > z \Rightarrow z < 2$$

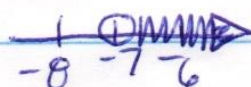


$$3. 5(12 - 3n) < 165$$

$$60 - 15n < 165$$

$$-15n < 105$$

$$n > -7$$



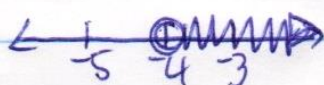
$$4. 18 - 4k < 2(k + 21)$$

$$18 - 4k < 2k + 42$$

$$18 < 6k + 42$$

$$-24 < 6k$$

$$-4 < k \Rightarrow k > -4$$



$$5. 4(b - 7) + 6 < 22$$

$$4b - 28 + 6 < 22$$

$$4b - 22 < 22$$

$$4b < 44$$

$$b < 11$$



$$6. 2 + 3(m + 5) \geq 4(m + 3)$$

$$2 + 3m + 15 \geq 4m + 12$$

$$3m + 17 \geq 4m + 12$$

$$17 \geq m + 12$$

$$5 \geq m \Rightarrow m \leq 5$$



7. Jim: \$5.75/hr 26% of total pay is deducted  $\geq 110$ /wk

$$5.75h - .26(5.75h) \geq 110$$

$$5.75h - 1.50h \geq 110$$

$$4.25h \geq 110$$

$$h \geq 25.88$$

He needs to work at least 26 hours a week