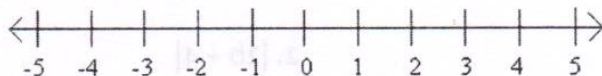


1-4 Solving Absolute Value Equations

Absolute Value of x : $|x|$ = the distance the number is from zero on a number line.

Since this value is a distance it can never be negative!



Intro: If $|2| = \underline{\quad}$ and $|-2| = \underline{\quad}$, then what is x if $|x| = 5$? $x = \underline{\quad}$ or $x = \underline{\quad}$

Steps to Evaluate an Expression with an Absolute Value:

1. Replace the variable with the given value.
2. Follow the order of operations to simplify the expression.

Examples:

1. $2.7 + |6 - 2x|$ if $x = 4$
2. $2.3 - |3y - 10|$ if $y = 2$

Always follow these steps for success!

Steps to Solving Absolute Value Equations:

1. Isolate the absolute value on one side of the equation.
2. Check to make sure that the equation is possible!! $|x| \neq -\#$
3. Set up two equations, considering both the positive and negative values:
 - Drop the absolute value and keep the sign of the expression on the right.
 - Drop the absolute value and switch the sign of the expression on the right.
4. Solve both equations.
5. Check both solutions with the original equation. Even if the correct procedure is used, the answers may not be actual solutions to the original equation. Such a number is called an **extraneous solution**.
6. Write your final answer. Because the absolute value of a number is always positive or zero, an equation like $|x| = -4$ is never true. This means it has no solution and would be an **empty set** written $\{\}$ or \emptyset .

Example:

$$|11 + 2x| = 5$$

$$\begin{array}{l} 11 + 2x = 5 \\ 2x = -6 \\ x = -3 \end{array} \quad \begin{array}{l} 11 + 2x = -5 \\ 2x = -16 \\ x = -8 \end{array}$$

Check your solution:

$$\begin{array}{l} |11 + 2(-3)| = 5 \\ |11 - 6| = 5 \\ |5| = 5 \\ 5 = 5 \end{array} \quad \begin{array}{l} |11 + 2(-8)| = 5 \\ |11 - 16| = 5 \\ |-5| = 5 \\ 5 = 5 \end{array}$$

Therefore, $x = -3$ and $x = -8$ or $\{-8, -3\}$

Examples: Solve each equation. Check your solution before writing your final answer

1. $|2x + 5| = 15$

$$\begin{array}{l} 2x + 5 = 15 \\ 2x = 10 \\ x = 5 \end{array} \quad \begin{array}{l} 2x + 5 = -15 \\ 2x = -20 \\ x = -10 \end{array}$$

Check: $|15| = 15$ ✓
 $|2(-10) + 5| = 15$ ✓
 Final answer: $\{-10, 5\}$

2. $-3|6 - 4t| - 6 = 0$

$$\begin{array}{l} -3|6 - 4t| = 6 \\ |6 - 4t| = -2 \end{array}$$

$\{\}$
or \emptyset

an absolute value can never = a -#!

3. $|3x - 5| = 2x + 1$

$$\begin{array}{l} 3x - 5 = 2x + 1 \\ x = 6 \end{array} \quad \begin{array}{l} 3x - 5 = -(2x + 1) \\ 3x - 5 = -2x - 1 \\ 5x = 4 \\ x = \frac{4}{5} \end{array}$$

Check: $|18 - 5| = 13$ ✓
 $|12 - 5| = 7$ ✓
 Final answer: $\{6\}$

Check: $|\frac{12}{5} - 5| = \frac{8}{5} - 1$ ✓
 $|\frac{12}{5} - 5| = \frac{8}{5} - 1$ ✓
 Final answer: \emptyset

