

FUJI

I would solve these by Factoring, Completing the square or Square roots

1-9: Solve each quadratic using the quadratic formula. Write irrational answers in simplified radical form.

1. $7x^2 - 5x = 0$
 $x = \frac{5 \pm \sqrt{25 - 4(0)}}{14}$
 $\frac{5 + \sqrt{25}}{14} = \frac{10}{14} = \frac{5}{7}$
 $\frac{5 - \sqrt{25}}{14} = \frac{0}{14} = 0$
 $\{0, \frac{5}{7}\}$

2. $4x^2 - 9 = 0$
 $0 \pm \sqrt{0 - 4(-36)}$
 $= \frac{\pm 8}{8}$
 $\frac{12}{8} \pm \frac{-12}{8}$
 $\{\pm \frac{3}{2}\}$

3. $3x^2 + 8x = 3$ $3x^2 + 8x - 3 = 0$
 $x = \frac{-8 \pm \sqrt{64 - 4(-9)}}{6}$
 $\frac{-8 \pm \sqrt{100}}{6}$
 $\frac{-8 + 10}{6} = \frac{2}{6}$
 $\frac{-8 - 10}{6} = \frac{-18}{6} = -3$
 $\{-3, \frac{1}{3}\}$

4. $25x^2 - 20x - 6 = 0$
 $x = \frac{20 \pm \sqrt{400 - 4(-150)}}{50}$
 $\frac{20 \pm \sqrt{1000}}{50}$
 $\frac{20 \pm 10\sqrt{10}}{50} = \frac{2 \pm \sqrt{10}}{5}$

5. $x^2 = 4x - 15$ $x^2 - 4x + 15 = 0$
 $x = \frac{4 \pm \sqrt{16 - 4(15)}}{2}$
 $\frac{4 \pm \sqrt{-44}}{2}$
 $\frac{4 \pm 2i\sqrt{11}}{2} = 2 \pm i\sqrt{11}$

6. $7x^2 + 6x + 2 = 0$
 $x = \frac{-6 \pm \sqrt{36 - 4(14)}}{14}$
 $\frac{-6 \pm \sqrt{-20}}{14}$
 $\frac{-6 \pm 2i\sqrt{5}}{14} = \frac{-3 \pm i\sqrt{5}}{7}$

7. $6x^2 - 2x = 1$ $6x^2 - 2x - 1 = 0$
 $x = \frac{2 \pm \sqrt{4 - 4(-6)}}{12}$
 $\frac{2 \pm \sqrt{28}}{12}$
 $\frac{2 \pm 2\sqrt{7}}{12} = \frac{1 \pm \sqrt{7}}{6}$

8. $16x^2 - 8x + 1 = 0$
 $x = \frac{8 \pm \sqrt{64 - 4(16)}}{32}$
 $\frac{8 \pm \sqrt{0}}{32}$
 $= \frac{8}{32} = \frac{1}{4}$ double root

9. $3x^2 + 36 = 0$
 $x = \frac{0 \pm \sqrt{0 - 4(108)}}{6}$
 $\frac{\pm \sqrt{-432}}{6} = \frac{\pm i\sqrt{16 \cdot 9 \cdot 3}}{6}$
 $\frac{\pm 12i\sqrt{3}}{6} = \pm 2i\sqrt{3}$

10-13: Find the value of the discriminant and describe the number and type of roots. DO NOT SOLVE!

10. $9x^2 - 6x + 1 = 0$
 $36 - 4(9)$
0: double root

11. $x^2 + 12x + 4 = 0$
 $144 - 4(4)$
128: 2 real irrational roots

12. $4x^2 - 4x + 11 = 0$
 $16 - 4(44)$
-160: 2 complex imaginary roots

13. $2x^2 - 7x - 4 = 0$
 $49 - 4(-8)$
81: 2 real rational roots

14. GRAVITATION - YOU MUST SOLVE THIS ALGEBRAICALLY!

The height $h(t)$ in feet of an object t seconds after it is propelled straight up from the ground with an initial velocity of 60 feet per second is modeled by the equation $h(t) = -16t^2 + 60t$. At what times will the object be at a height of 56 feet?

$56 = -16t^2 + 60t \rightarrow 16t^2 - 60t + 56 = 0$
 $\frac{60 \pm \sqrt{3600 - 4(896)}}{32} = \frac{60 \pm \sqrt{16}}{32}$
 $\frac{60 + 4}{32} = \frac{64}{32} = 2$ $\frac{60 - 4}{32} = \frac{56}{32} = 1.75$
at 1.75 & 2 seconds