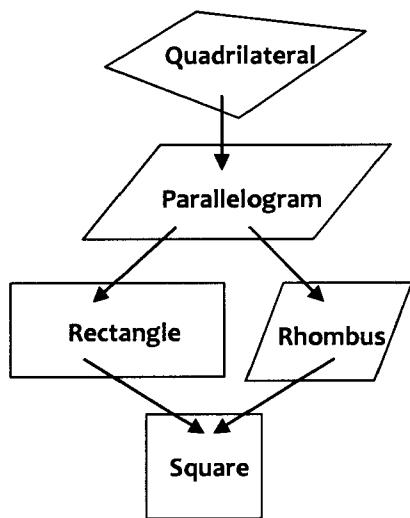
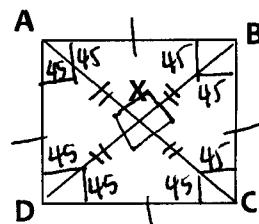
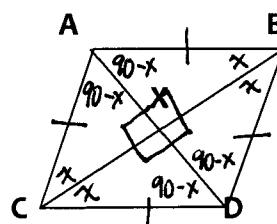
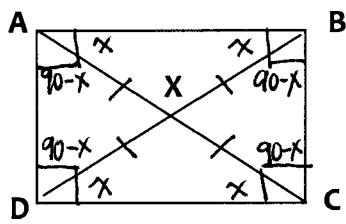


# Master 6-5 Rhombi & Squares



- If I want a quadrilateral to become a parallelogram, what must I do?  
Make 2 pr. of opp. sides parallel
- If I want a parallelogram to become a rectangle, what must I do?  
Make all 4 angles right angles
- If I want a parallelogram to become a rhombus, what must I do?  
Make all 4 sides  $\cong$
- If I want a parallelogram to become a square, what must I do?  
Make all 4 sides  $\cong$  & angles  $\cong$

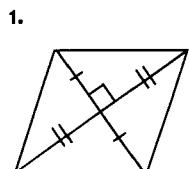
Now let's look at the properties that differentiate a rectangle, rhombus, and square.



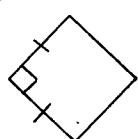
| Rectangle             | Rhombus                          | Square                           |
|-----------------------|----------------------------------|----------------------------------|
| 4 right angles        | 4 $\cong$ sides                  | 4 right angles                   |
| Diagonals are $\cong$ | Diagonals are $\perp$            | 4 $\cong$ sides                  |
|                       | Diagonals bisect opp. $\angle$ s | Diagonals are $\cong$            |
|                       |                                  | Diagonals are $\perp$            |
|                       |                                  | Diagonals bisect opp. $\angle$ s |

You must commit these properties to memory in order to know the best name for your parallelogram!

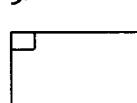
1-6: Each figure is a parallelogram. Identify the special type and explain your reasoning.



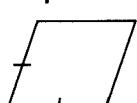
Rhombus  
 $\square$  w/  $\perp$  diag.



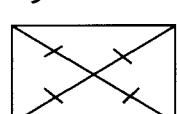
Square  
Rhomb.  
w/ rt.  $\angle$ s



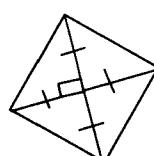
Rectangle  
 $\square$  w/ rt.  $\angle$ s



Rhombus  
 $\square$  w/  
 $\cong$  sides



Rectangle  
 $\square$ ,  
Diag  $\cong$



Square  
 $\cong$  Diag = Rect.  
 $\perp$  Diag = Rhomb.  
Rect + Rhom = Sq!

7-12: Match the properties of a quadrilateral with all of the types of quadrilaterals which have that property.

B & D

7. The diagonals are congruent.

A. Parallelogram

A - D

8. Both pairs of opposite sides are congruent.

B. Rectangle

A - D

9. Both pairs of opposite sides are parallel.

C. Rhombus

B & D

10. All angles are congruent.

D. Square

C & D

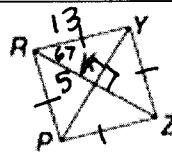
11. All sides are congruent.

C & D

12. Diagonals bisect the angles.

13-16: Given rhombus PRYZ,  $RK = 5$ ,  $RY = 13$ , and  $m\angle YRZ = 67^\circ$ , find each measure.

13.  $KY = \underline{12}$



14.  $PK = \underline{12} \quad KY = PK$

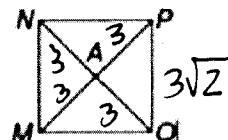
$$\begin{aligned} RY^2 &= RK^2 + KY^2 \\ 13^2 &= 5^2 + KY^2 \\ 169 &= 25 + KY^2 \\ 144 &= KY^2 \\ KY &= 12 \end{aligned}$$

15.  $m\angle YKZ = \underline{90^\circ}$  Diag. are  $\perp$

16.  $m\angle PZR = \underline{67^\circ}$  Alt. int.  $\nexists \cong$

17-20: Given square MNPQ,  $PQ = 3\sqrt{2}$ , find each measure.

17.  $AQ = \underline{3} \quad 45-45-90 \Delta$



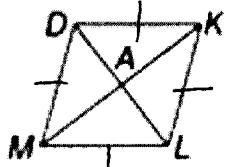
18.  $PM = \underline{6}$

19.  $m\angle APQ = \underline{45^\circ}$  All  $90^\circ \nexists$  are bisected to form  $45^\circ \nexists$

20.  $m\angle MNP = \underline{90^\circ}$  All angles are rt  $\nexists$

21-25: Given rhombus DKLM, find each measure.

21. If  $DK = 8$ , then  $KL = \underline{8}$ . All sides are  $\cong$



22. If  $m\angle DML = 82$ , then  $m\angle DKM = \underline{41^\circ}$ .  $\begin{array}{c} ? \\ 82 \end{array}$   $\nexists$ s are bisected by the diagonals

23. If  $m\angle KAL = 2x - 8$ , then  $x = \underline{49}$ .  $2x - 8 = 90$   
 $2x = 98$

24. If  $DA = 4x$  and  $AL = 5x - 3$ , then  $DL = \underline{24}$  and  $AD = \underline{12}$ .  $4x = 5x - 3$   
 $-x = -3$   
 $12 + 12 = 24$

25. If  $DM = 5y + 2$  and  $DK = 3y + 6$ , then  $KL = \underline{12}$ .  $5y + 2 = 3y + 6$   
 $2y = 4$   
 $y = 2$   $KL = DK = 3(2) + 6$

26: Given the edges of a window shown below, decide if the window is a square or rhombus. Justify your answer!

$m\overline{AB} = \frac{6}{5}$

$\overline{AB} \not\parallel \overline{BC}$   
bc the slopes

$AB = \sqrt{36 + 25} = \sqrt{61}$

$m\overline{BC} = \frac{6}{5}$

are not opp  
reciprocals,

$BC = \sqrt{36 + 25} = \sqrt{61}$

$m\overline{CD} = \frac{6}{5}$

so it is  
NOT a square

It is a rhombus bc  
a  $\square$  w/ consec. sides  
 $\cong$  will be a rhombus!

$m\overline{AD} = \frac{6}{5}$

$\square$  bc opp  
sides  $\parallel$

