

Day 02 Graphing Reciprocal Functions

Name _____ Date _____ Block _____

Reciprocal Function: $f(x) = \frac{1}{a(x)}$, where $a(x)$ is a linear function and $a(x) \neq 0$

Parent Function:

$$f(x) = \frac{1}{x}$$

Type of Graph:

Hyperbola

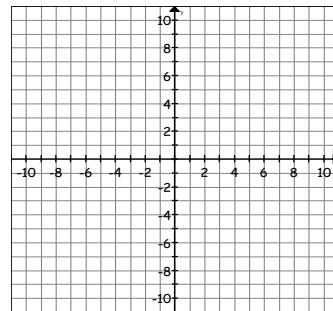
Asymptotes:

Vertical: $x = 0$

Horizontal: $y = 0$

Domain & Range:

$$(-\infty, 0) \cup (0, +\infty)$$



KeyConcept Transformations of Reciprocal Functions

$$f(x) = \frac{a}{x-h} + k$$

h – Horizontal Translation

h units right if *h* is positive

|*h*| units left if *h* is negative

The *vertical* asymptote is at $x = h$.

k – Vertical Translation

k units up if *k* is positive

|*k*| units down if *k* is negative

The *horizontal* asymptote is at $f(x) = k$.

a – Orientation and Shape

If $|a| < 1$, the graph is reflected across the *x*-axis.

If $|a| > 1$, the graph is stretched vertically.

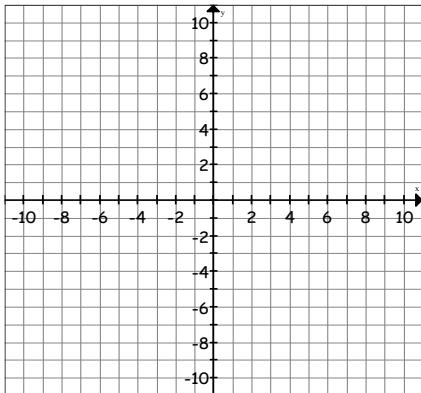
If $0 < |a| < 1$, the graph is compressed vertically.

How to graph a rational function:

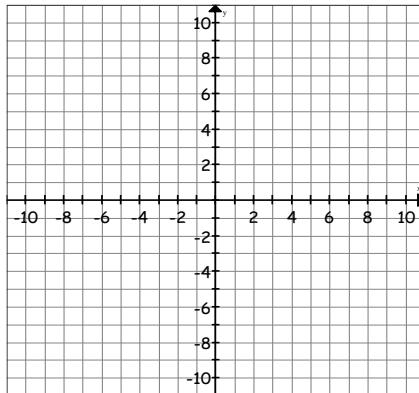
- Find the equations of the asymptotes and draw them on the graph.
- Find at least two points on each “branch” of the graph. Draw the branches of the hyperbola through the points and approaching the asymptotes.

Graph each function. Then state the asymptotes, domain and range of each.

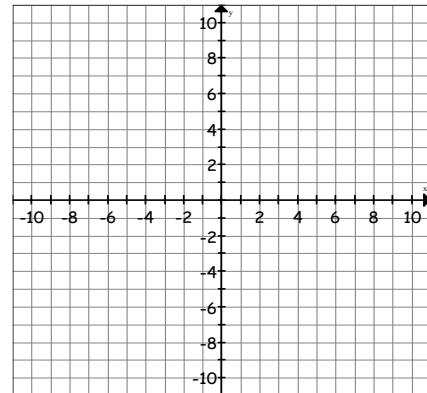
1. $f(x) = \frac{2}{x}$



2. $f(x) = \frac{-2}{x}$



3. $f(x) = \frac{2}{x-3} + 1$



asympt: H: _____ V: _____

domain: _____

range: _____

asympt: H: _____ V: _____

domain: _____

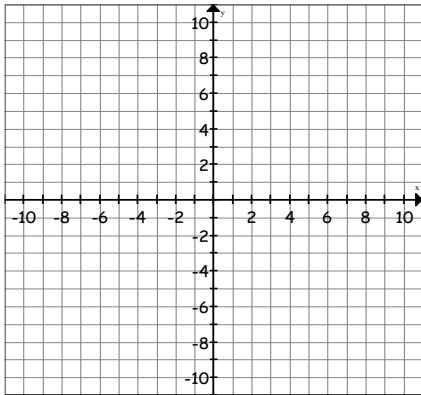
range: _____

asympt: H: _____ V: _____

domain: _____

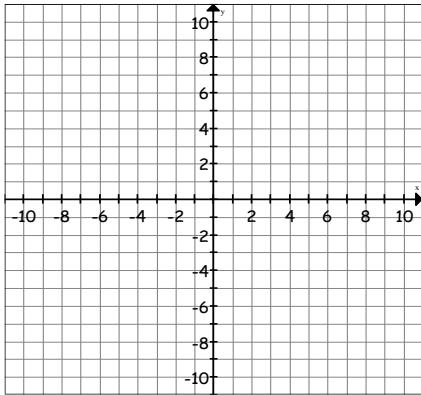
range: _____

4. $f(x) = \frac{1}{x+5} - 2$



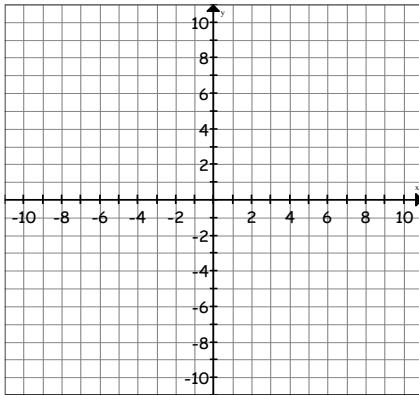
asymptote: H: _____ V: _____
 domain: _____
 range: _____

7. $f(x) = \frac{1}{x-1} - 5$



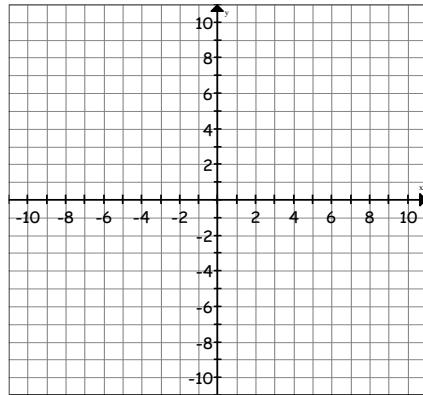
asymptote: H: _____ V: _____
 domain: _____
 range: _____

5. $f(x) = \frac{-3}{x+2} - 1$



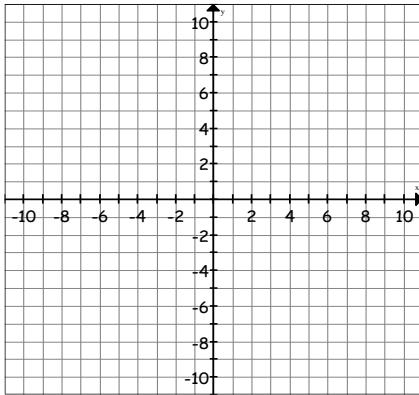
asymptote: H: _____ V: _____
 domain: _____
 range: _____

6. $f(x) = \frac{2}{x-1} - 4$



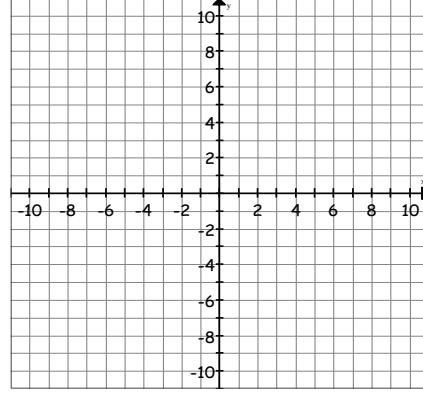
asymptote: H: _____ V: _____
 domain: _____
 range: _____

8. $f(x) = \frac{-1}{x-3} - 4$



asymptote: H: _____ V: _____
 domain: _____
 range: _____

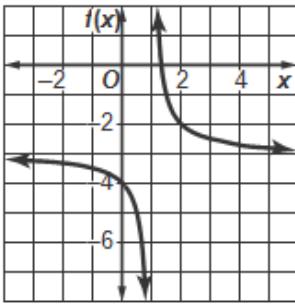
9. $f(x) = \frac{4}{x+3}$



asymptote: H: _____ V: _____
 domain: _____
 range: _____

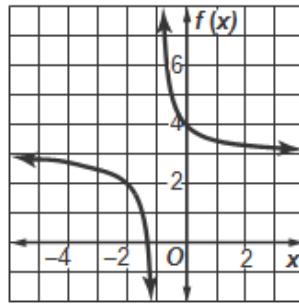
Find the asymptotes and the domain and range of each function. Then complete the equation.

10. $f(x) = \frac{1}{x}$



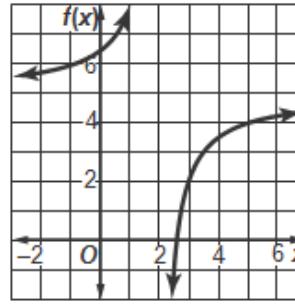
asymptote: H: _____ V: _____
 domain: _____
 range: _____

11. $f(x) = \frac{1}{x^2}$



asymptote: H: _____ V: _____
 domain: _____
 range: _____

12. $f(x) = \frac{-3}{x-2}$



asymptote: H: _____ V: _____
 domain: _____
 range: _____