

Graphing Rational Functions

1-4: Simplify each expression.

1) $\frac{x^2 + 17x + 72}{10x + 90} \cdot \frac{(x+9)(x+8)}{10(x+9)}$

$\frac{x+8}{10}$

2) $\frac{1}{n-9} \cdot \frac{2n^3 - 18n^2}{5}$

$\frac{1}{(n-9)} \cdot \frac{2n^2(n-9)}{5} = \frac{2n^2}{5}$

3) $\frac{1}{7x-14} \div \frac{x+1}{6x^3+6x^2}$

$\frac{1}{7(x-2)} \div \frac{(x+1)}{6x^2(x+1)}$
 $\frac{1}{7(x-2)} \cdot \frac{6x^2(x+1)}{(x+1)} = \frac{6x^2}{7(x-2)}$

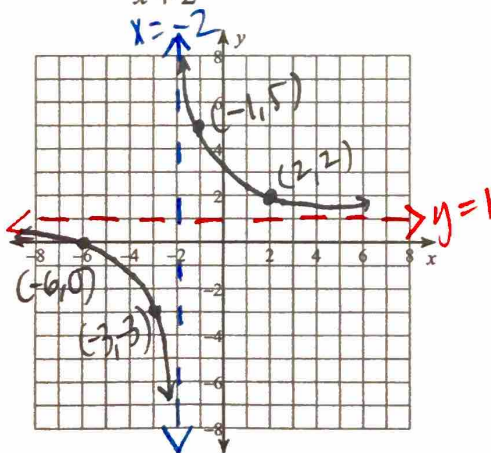
4) $\frac{y \cdot 6x}{y \cdot 2} + \frac{2x}{2y}$

LCD = 2y

$\frac{6xy}{2y} + \frac{2x}{2y} = \frac{6xy+2x}{2y} = \frac{2x(6y+1)}{2y} = \frac{x(6y+1)}{y}$

5-10: Identify the vertical asymptotes, horizontal asymptote, domain, and range of each. Then sketch the graph.

5) $f(x) = \frac{4}{x+2} + 1$



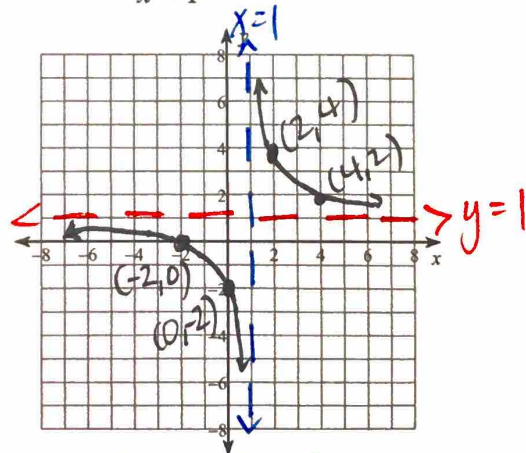
V.A.: $x = -2$

H.A.: $y = 1$

D: $(-\infty, -2) \cup (-2, \infty)$ or $\mathbb{R}, x \neq -2$

R: $(-\infty, 1) \cup (1, \infty)$ or $\mathbb{R}, y \neq 1$

6) $f(x) = \frac{3}{x-1} + 1$



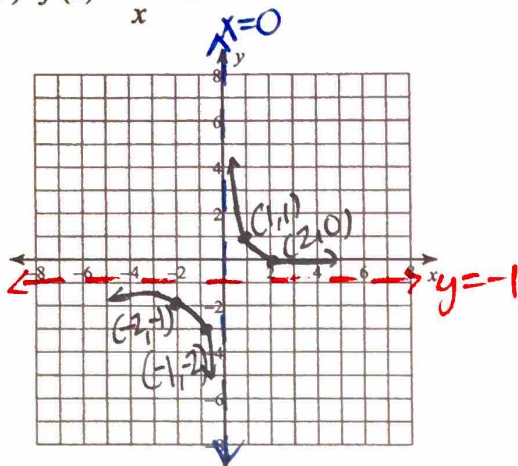
V.A.: $x = 1$

H.A.: $y = 1$

D: $(-\infty, 1) \cup (1, \infty)$ or $\mathbb{R}, x \neq 1$

R: $(-\infty, 1) \cup (1, \infty)$ or $\mathbb{R}, y \neq 1$

7) $f(x) = \frac{2}{x} - 1$



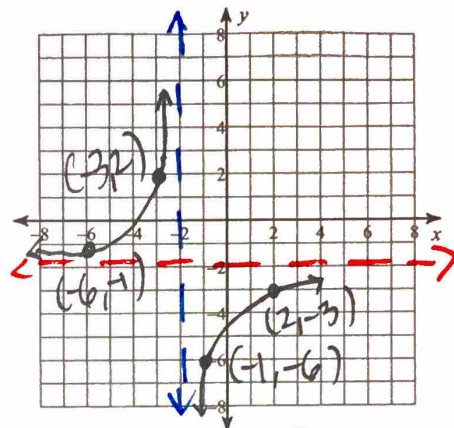
V.A.: $x=0$

H.A.: $y=-1$

D: $(-\infty, 0) \cup (0, \infty)$ or $\mathbb{R}, x \neq 0$

R: $(-\infty, -1) \cup (-1, \infty)$ or $\mathbb{R}, y \neq -1$

8) $f(x) = -\frac{4}{x+2} - 2$



V.A.: $x=-2$

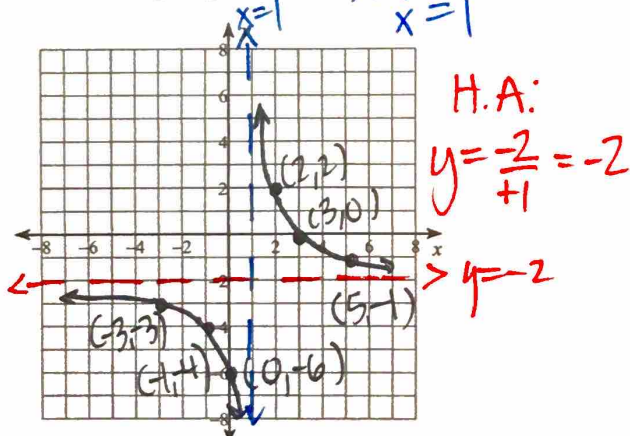
H.A.: $y=-2$

D: $(-\infty, -2) \cup (-2, \infty)$ or $\mathbb{R}, x \neq -2$

R: $(-\infty, -2) \cup (-2, \infty)$ or $\mathbb{R}, y \neq -2$

9) $f(x) = \frac{-2x+6}{x-1}$

V.A.: $x-1=0$
 $x=1$



H.A.: $y = \frac{-2}{+1} = -2$

$y = -2$

V.A.: $x=1$

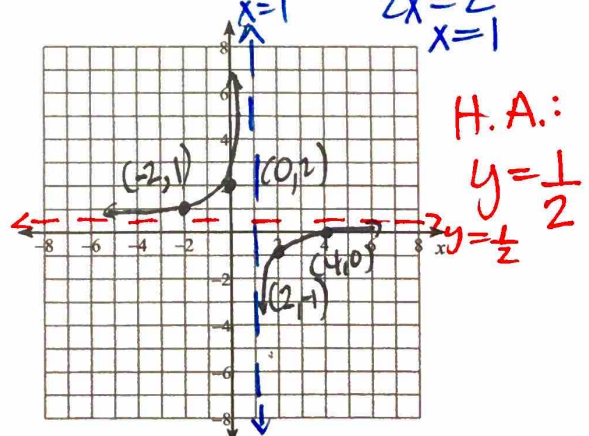
H.A.: $y=-2$

D: $(-\infty, 1) \cup (1, \infty)$ or $\mathbb{R}, x \neq 1$

R: $(-\infty, -2) \cup (-2, \infty)$ or $\mathbb{R}, y \neq -2$

10) $f(x) = \frac{x-4}{2x-2}$

V.A.: $2x-2=0$
 $2x=2$
 $x=1$



H.A.: $y = \frac{1}{2}$

$y = \frac{1}{2}$

V.A.: $x=1$

H.A.: $y = \frac{1}{2}$

D: $(-\infty, 1) \cup (1, \infty)$ or $\mathbb{R}, x \neq 1$

R: $(-\infty, \frac{1}{2}) \cup (\frac{1}{2}, \infty)$ or $\mathbb{R}, y \neq \frac{1}{2}$