

Rational Exponents

If an exponent is a fraction, the numerator represents the **power** and the denominator represents the **root**.

$\sqrt[n]{a^x} = \left(\sqrt[n]{a}\right)^x = a^{\frac{x}{n}}$	
$(\text{base})^{\frac{\text{power}}{\text{root}}}$	$3^{\frac{3}{2}} = \sqrt{3^3} = \sqrt{3^2 \cdot 3} = 3\sqrt{3}$

1-8: Rewrite each expression using rational exponent notation.

1. $\sqrt[5]{x^2}$ 2. $\sqrt[3]{5}$ 3. $\sqrt[6]{16}$ 4. $\sqrt[10]{x^8}$

5. $\sqrt{36x^5y^7}$ 6. $\sqrt[4]{16a^2b^3}$ 7. $\sqrt[3]{28x^2y^4z^3}$ 8. $3\sqrt[4]{8n^{11}w^2}$

9-13: Rewrite each expression using radical notation.

9. $5^{\frac{2}{3}}$ 10. $41^{\frac{2}{7}}$ 11. $(216)^{\frac{4}{3}}$ 12. $16^{-\frac{5}{3}}$ 13. $(256)^{-\frac{7}{6}}$

14-18: Rewrite each expression USING A CALCULATOR. Round results to the nearest hundredth.

14. $(36)^{\frac{5}{2}}$ 15. $(-12)^{-\frac{1}{3}}$ 16. $(\sqrt[3]{28})^7$ 17. $(\sqrt[5]{3})^{-4}$ 18. $(\sqrt[4]{22^3})$

19-23: Evaluate each expression WITHOUT USING A CALCULATOR.

19. $\sqrt[3]{125}$ 20. $\sqrt[4]{81^3}$ 21. $49^{-\frac{3}{2}}$ 22. $-27^{\frac{2}{3}}$ 23. $(\sqrt[3]{-64})^2$

24-35: Simplify each expression completely. Write your final answer in simplest radical form.

24. $\sqrt[5]{7a^{10}b^7c^{10}}$

25. $\sqrt[4]{16d^4e^{10}f^{15}}$

26. $\sqrt[4]{(x+2)^4}$

27. $\sqrt[6]{128x^4y^{13}z^7}$

28. $\sqrt[3]{-64(x-1)^6}$

29. $\sqrt{25(x+6)^{10}}$

30. $3^{\frac{1}{3}}x^{\frac{1}{4}}y^{\frac{5}{6}}z^{\frac{4}{3}}$

31. $(25g^5h^4)^{\frac{1}{2}}$

32. $(256j^{16}k^2l^{10})^{\frac{1}{4}}$

33. $\frac{\sqrt[3]{36xy^2}}{\sqrt[3]{10xz}}$

34. $\sqrt[4]{48a^9b^3c^{16}}$

35. $\frac{1}{3^{\frac{1}{2}}}$