

Master E

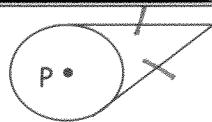
WARM-UP/REVIEW of Unit 8 (Chapter 10) – Circles

Vocabulary: You must know these terms/definitions and be able to identify them when given a picture of a circle.

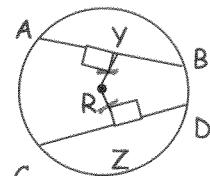
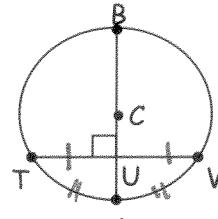
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|----------------------|--------------------------|-----------------------|--------------------------|
| 1. circle | 8. tangent | 14. circumference | 19. circumscribed circle |
| 2. center | 9. interior of a circle | 15. arc length | 20. tangent segment |
| 3. radius | 10. exterior of a circle | 14. semicircle | 21. secant segment |
| 4. congruent circles | 11. point of tangency | 15. congruent arcs | 22. external secant seg. |
| 5. diameter | 12. central angle | 16. inscribed angle | 23. common tangent |
| 6. chord | 13. minor arc | 17. intercepted arc | 24. concentric circles |
| 7. secant | 18. major arc | 18. inscribed polygon | 25. sector/area |

Theorems: Label the appropriate picture to illustrate the theorem.

- ◆ Tangents to a circle from the same exterior point are \cong to each other.

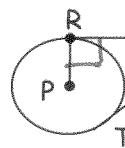


- ◆ If a radius is perpendicular to a chord, it bisects the chord and its arc.



- ◆ Two chords are congruent if they are equidistant from the center.
 $AB \cong CD$

- ◆ A tangent is perpendicular to the radius at the point of tangency.



- ◆ If 2 chords are congruent, then the arcs they form are congruent also.

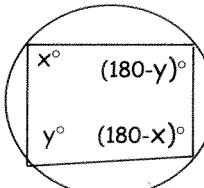
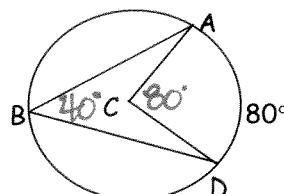
- ◆ Circumference of a circle is $2\pi r$ or πd . Area of a circle is πr^2 .

- ◆ The arc length of a circle (l) is part of the circumference of a circle. Formula: $l = \frac{m}{360} \cdot 2\pi r$

- ◆ The area of a sector of a circle (A) is the part of the area of a circle. Formula: $A = \frac{m}{360} \cdot \pi r^2$

Angles: Memorize the formulas for each scenario.

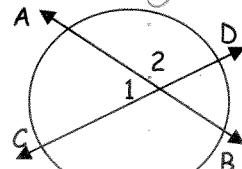
- ◆ A central angle is \cong to its arc.



- ◆ An inscribed angle is half the measure of its arc.

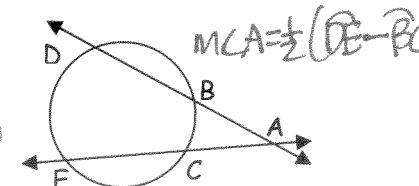
Supplementary

- ◆ The opposite angles of an inscribed quadrilateral are supplementary.



- ◆ An angle inside the circle is half the sum of its arcs.

$$m\angle 1 = \frac{1}{2}(AC + BD)$$



- ◆ An angle outside the circle is half the difference of its arcs.

Segments:

Memorize the formulas for each scenario.

- 2 chords in a circle form 4 segments: $\frac{\text{part}}{\text{whole}} \times \frac{\text{part}}{\text{whole}} = \frac{\text{part}}{\text{whole}} \times \frac{\text{part}}{\text{whole}}$

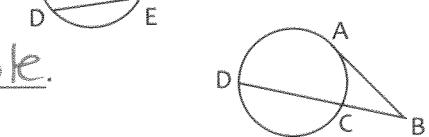
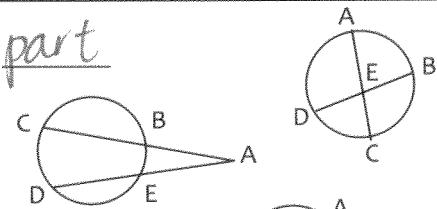
$$AE \cdot EC = DE \cdot EB$$

- 2 secant segments: $\frac{\text{part}}{\text{whole}} \times \frac{\text{whole}}{\text{whole}} = \frac{\text{part}}{\text{whole}} \times \frac{\text{whole}}{\text{whole}}$.

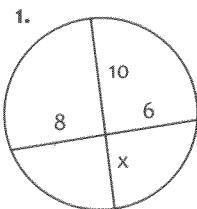
$$AB \cdot AC = AE \cdot AD$$

- A tangent and a secant segment: tangent squared = part times whole.

$$AB^2 = BC \cdot BD$$

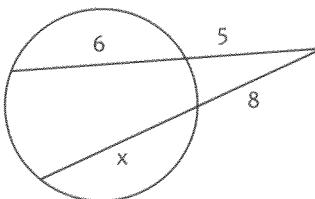


PRACTICE:

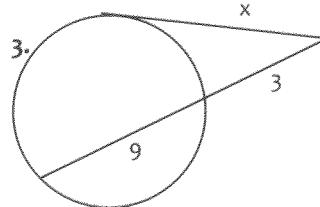


$$\begin{aligned} 10x &= 8 \cdot 6 \\ 10x &= 48 \\ x &= 4.8 \end{aligned}$$

* 2.

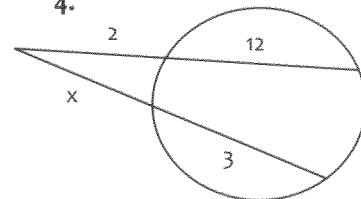


$$\begin{aligned} 5(11) &= 8(x+8) \\ 55 &= 8x + 64 \\ -9 &= 8x \\ -\frac{9}{8} &= x \end{aligned}$$



$$\begin{aligned} x^2 &= 3(12) \\ x^2 &= 36 \\ x &= 6 \end{aligned}$$

4.



$$\begin{aligned} x(x+3) &= 2(14) \\ x^2 + 3x &= 28 \\ x^2 + 3x - 28 &= 0 \\ (x+7)(x-4) &= 0 \\ x &= -7 \quad x = 4 \end{aligned}$$

Equations of a circle: Formula: $(x - h)^2 + (y - k)^2 = r^2$

PRACTICE:

5. Write an equation for a circle with a center at the origin and $r = 6$

$$x^2 + y^2 = 36$$

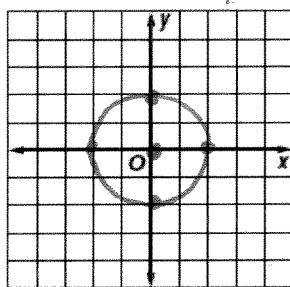
6. Write an equation for the circle with a center at $(4, 3)$ and $d = 10$

$$r=5$$

$$(x-4)^2 + (y-3)^2 = 25$$

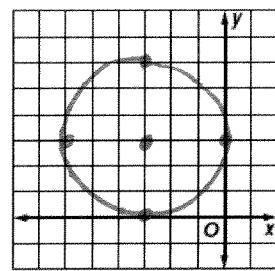
7. Graph the circle below.

$$x^2 + y^2 = 4$$



8. Graph the circle below.

$$(x + 3)^2 + (y - 3)^2 = 9$$



$$\begin{aligned} C(-3, 3) \\ r=3 \end{aligned}$$